

Cambridge International AS Level

MATHEMATICS
Paper 2 Pure Mathematics 2
MARK SCHEME
Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2024 series for most Cambridge IGCSE, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always whole marks (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics Specific Marking Principles

- Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

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Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- **B** Mark for a correct result or statement independent of method marks.
- DM or DB When a part of a question has two or more 'method' steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.
- A or B marks are given for correct work only (not for results obtained from incorrect working) unless follow through is allowed (see abbreviation FT above).
- For a numerical answer, allow the A or B mark if the answer is correct to 3 significant figures or would be correct to 3 significant figures if rounded (1 decimal place for angles in degrees).
- The total number of marks available for each question is shown at the bottom of the Marks column.
- Wrong or missing units in an answer should not result in loss of marks unless the guidance indicates otherwise.
- Square brackets [] around text or numbers show extra information not needed for the mark to be awarded.

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Abbreviations

AEF/OE Any Equivalent Form (of answer is equally acceptable) / Or Equivalent

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

CAO Correct Answer Only (emphasising that no 'follow through' from a previous error is allowed)

CWO Correct Working Only

ISW Ignore Subsequent Working

SOI Seen Or Implied

SC Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the

light of a particular circumstance)

WWW Without Wrong Working

AWRT Answer Which Rounds To

Question	Answer	Marks	Guidance
1	Differentiate to obtain $2\sec^2 x - 5\cos x$	B1	
	Equate first derivative to zero and solve correctly at least as far as $\cos x =$	M1	B1 M1 for $x = 42.5^{\circ}$.
	Obtain $\cos x = \sqrt[3]{0.4}$ and hence $x = 0.742$	A1	Or greater accuracy (0.74261).
		3	

Question	Answer	Marks	Guidance
2	Attempt use of product rule for differentiating $x^2 \ln y$	M1	Allow if $\frac{dy}{dx}$ missing.
	Obtain $2x \ln y + \frac{x^2}{y} \frac{dy}{dx}$	A1	
	Obtain $+2y\frac{dy}{dx}$	B1	
	Substitute $x = 2$, $y = 1$ in equation equal to 0 involving at least one $\frac{dy}{dx}$ and solve for $\frac{dy}{dx}$	M1	Correct equation: $2x \ln y + \frac{x^2}{y} \frac{dy}{dx} + 2y \frac{dy}{dx} + 4 = 0$
	Obtain $-\frac{2}{3}$	A1	Or exact equivalent. Not from wrong working.
		5	

Question	Answer	Marks	Guidance
3(a)	Draw V-shaped graph with vertex on positive x-axis in the first quadrant.	B1	
	Draw correct graph of $y = 5 - x$ correctly positioned with respect to modulus graph.	B1	Two points of intersection.
		2	
3(b)	Solve $3x - 8 = 5 - x$ to obtain $\frac{13}{4}$	B1	Or inequality.
	Solve linear equation or inequality with signs of $3x$ and x the same	M1	
	Obtain $\frac{3}{2}$	A1	
	Conclude $\frac{3}{2} < x < \frac{13}{4}$ or $x > \frac{3}{2}$ and $x < \frac{13}{4}$	A1	Allow alternative notation e.g. $\left(\frac{3}{2}, \frac{13}{4}\right)$.
	Alternative Method for Question 3(b)	1	
	State or imply non-modulus equation (or inequality) $(3x-8)^2 = (5-x)^2$	(B1)	
	Attempt solution of three-term equation (or inequality)	(M1)	
	Obtain $\frac{3}{2}$ and $\frac{13}{4}$	(A1)	
	Conclude $\frac{3}{2} < x < \frac{13}{4}$ or $x > \frac{3}{2}$ and $x < \frac{13}{4}$	(A1)	Allow alternative notation e.g. $\left(\frac{3}{2}, \frac{13}{4}\right)$.
		4	
3(c)	Attempt value of N (maybe non-integer at this stage) for $e^{0.1N} < their \frac{13}{4}$	M1	Allow $e^{0.1N} = their \frac{13}{4}$ (or inequality).
	Conclude with single integer 11	A1	
		2	

Question	Answer	Marks	Guidance	
4(a)	State $3 \tan 2\theta = \frac{6 \tan \theta}{1 - \tan^2 \theta}$	B1	Allow for $3\tan 2\theta = 3\left(\frac{2\tan \theta}{1-\tan^2 \theta}\right)$.	
	State $\tan(\theta + 45^\circ) = \frac{\tan \theta + 1}{1 - \tan \theta}$	B1		
	Attempt to express left-hand side in terms of $\tan \theta$ as a single fraction	M1	Condone sign errors in identities. Allow if tan 45° is not evaluated. Allow if 2 separate terms with a common denominator.	
	Confirm $\frac{\tan^2 \theta + 8 \tan \theta + 1}{1 - \tan^2 \theta}$	A1	Answer given – necessary detail needed.	
		4		
4(b)	Solve quadratic equation $5 \tan^2 \theta + 8 \tan \theta - 3 = 0$ to obtain at least one value of θ	M1	Must be using a correct method.	
	Obtain 17.4	A1	Or greater accuracy.	
	Obtain 117.6	A1	Or greater accuracy; and no others between 0° and 180° .	
		3		

Question	Answer	Marks	Guidance					
5(a)	Differentiate using quotient rule	*M1	OE					
	Obtain $\frac{(1+3x) 2e^{2x} - (1+e^{2x}) 3}{(1+3x)^2}$	A1	OE					
	Equate first derivative to zero and arrange as far as $x =$	DM1						
	Confirm $x = \frac{1}{6} + \frac{1}{2}e^{-2x}$	A1	Answer given – necessary detail needed. Must have exact terms.					
		4						
5(b)	b) Consider sign of $x - \frac{1}{6} - \frac{1}{2}e^{-2x}$		OE					
	Obtain -0.06 (- 0.064959) and 0.08 (0.0800) or equivalents and justify conclusion	A1	Answer given – necessary detail needed.					
	Alternative Method 1 for Question 5(b)							
	Consider $f(x) = \frac{1}{6} - \frac{1}{2}e^{-2x}$ and obtain $f(0.35) = 0.42$ (0.4149) and $f(0.45) = 0.37$ (0.36995)	(M1)						
	Conclude $f(0.35) < 0.45$ and $f(0.45) > 0.35$ so root lies in given interval.	(A1)						
	Alternative Method 2 for Question 5(b)							
	Consider the sign of their $\frac{dy}{dx}$ from part (a)	(M1)						
	Obtain -0.19 (- 0.187) and 0.21 (0.2139) or equivalents and justify conclusion	(A1)						
		2						

Question	Answer	Marks	Guidance
5(c)	Use iterative process correctly at least once	M1	
	Obtain final answer 0.394	A1	Answer required to exactly 3sf.
	Show sufficient iterations to 5 sf to justify answer or show sign change in interval [0.3935, 0.3945]	A1	
		3	

Question	Answer	Marks	Guidance
6(a)	Use y-values (0), $\sqrt{\sin\frac{1}{6}\pi + \sin^2\frac{1}{6}\pi}$, $\sqrt{\sin\frac{1}{3}\pi + \sin^2\frac{1}{3}\pi}$ or decimal equivalents	B1	(0), $\sqrt{0.75}$ or 0.866, $\sqrt{1.616}$ or 1.271.
	Use correct formula, or equivalent, with $h = \frac{1}{12}\pi$	M1	Must be using 'y' values. May do as 2 separate trapezia (0.113359 + 0.27976).
	Obtain 0.39	A1	Allow 0.393 but not greater accuracy.
		3	

Question	Answer Marks Guidance							
6(b)	Use $(\pi)\int (\sin 2x + \sin^2 2x) dx$	M1	OE					
	Express integrand in the form $k_1 \sin 2x + k_2 + k_3 \cos 4x$	*M1	Where $k_1 k_2 k_3 \neq 0$.					
	Obtain correct $\sin 2x + \frac{1}{2} - \frac{1}{2}\cos 4x$	A1	Or π times this.					
	Integrate to obtain $-\frac{1}{2}\cos 2x + \frac{1}{2}x - \frac{1}{8}\sin 4x$	A1 FT	Following <i>their</i> integrand only if of correct form.					
	Apply limits correctly to obtain exact value	DM1						
	Obtain volume = $\frac{1}{4}\pi + \frac{1}{12}\pi^2 - \frac{1}{16}\pi\sqrt{3}$	A1	Or exact equivalent.					
		6						

Question				Marks	Guidance				
7(a)	Carry out division at least as far as $3x^2 + n_1$						Or equivalent (inspection,).		
	Obtain quotient $3x^2 + 4$								
	Confirm remainder is $k-8$					A1	Answer given – necessary detail needed.		
						SC B1 for correct use of factor theorer show remainder is $k-8$.			
	Alternative Method for Question 7(a)					•			
	Synthetic division					(M1)	Allow one sign error.		
	-2/3	9	6	12	k				
			-6	0	-8				
		9	0	12	k-8				
	Obtain quotient $3x^2 + 4$					(A1)			
	Confirm	Confirm remainder is $k-8$				(A1)			
						3			

Question	Answer	Marks	Guidance	
7(b)	Integrate to obtain at least a term in x^3 and term of form $n_2 \ln(3x+2)$	*M1	Need to be using <i>their</i> answer to part (a).	
	Obtain $x^3 + 4x + \frac{1}{3}(k-8)\ln(3x+2)$	A1	FT on a quotient of $9x^2 + 12$.	
	Apply limits correctly to expression with three terms	DM1		
	Obtain $a = 235$	A1	FT on a quotient of $9x^2 + 12$.	
	Equate logarithm term to ln 64 and apply appropriate logarithm properties	DM1		
	Obtain $k = 17$	A1		
		6	SC 2 marks for use of quotient $3x^2 + 4$ or $9x^2 + 12$ to obtain either 235 or 705 if no other marks are available.	